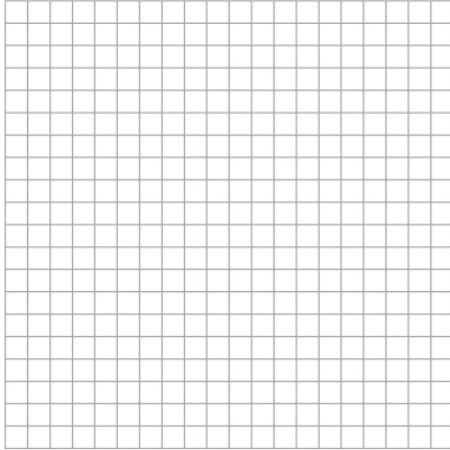


Name : _____

Characteristics of Quadratic Functions

Find the following characteristics of each graph.

① $f(x) = 2x^2 + 4x + 1$



Vertex:

Axis of Symmetry:

End behavior:

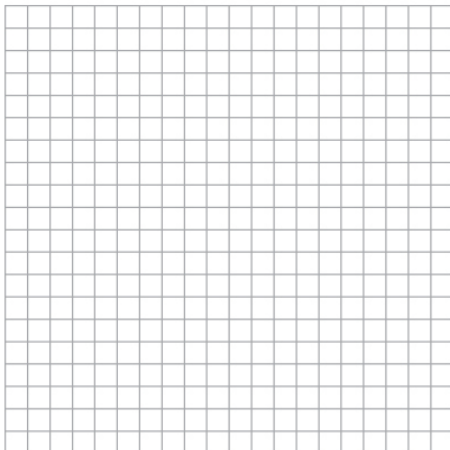
x-intercepts:

y-intercepts:

Domain:

Range:

② $f(x) = x^2 + 12x - 9$



Vertex:

Axis of Symmetry:

End behavior:

x-intercepts:

y-intercepts:

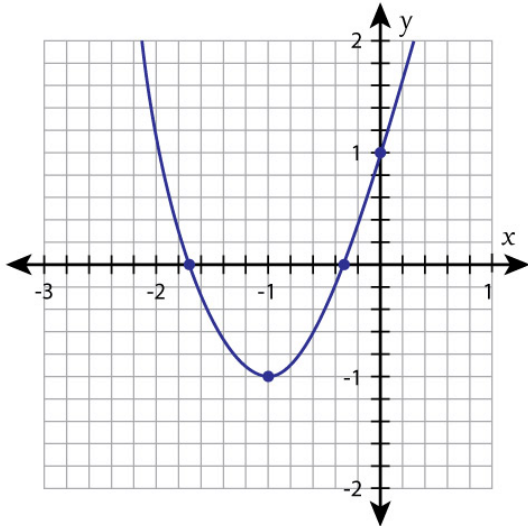
Domain:

Range:

Characteristics of Quadratic Functions

Answers

① $f(x) = 2x^2 + 4x + 1$



Vertex: $(-1, -1)$

Axis of Symmetry: $x = -1$

End behavior:

$x \rightarrow +\infty, f(x) \rightarrow +\infty$, and as $x \rightarrow -\infty, f(x) \rightarrow +\infty$

x-intercepts:

$$\left(\frac{-2 + \sqrt{2}}{2}, 0\right), \left(-\frac{\sqrt{2} + 1}{\sqrt{2}}, 0\right)$$

y-intercepts: $(0, 1)$

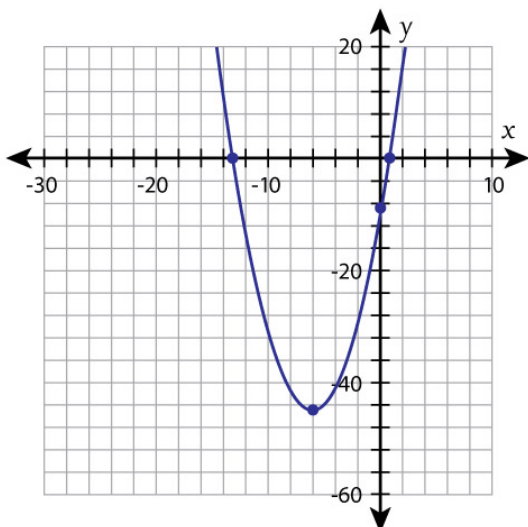
Domain:

$$\left[\begin{array}{l} \text{Solution: } -\infty < x < \infty \\ \text{Interval Notation: } (-\infty, \infty) \end{array} \right]$$

Range:

$$\left[\begin{array}{l} \text{Solution: } f(x) \geq -1 \\ \text{Interval Notation: } [-1, \infty) \end{array} \right]$$

② $f(x) = x^2 + 12x - 9$



Vertex: $(-6, -45)$

Axis of Symmetry: $x = -6$

End behavior:

$x \rightarrow +\infty, f(x) \rightarrow +\infty$, and as $x \rightarrow -\infty, f(x) \rightarrow +\infty$

x-intercepts:

$$(3(\sqrt{5} - 2), 0), (-3(2 + \sqrt{5}), 0)$$

y-intercepts: $(0, -9)$

Domain:

$$\left[\begin{array}{l} \text{Solution: } -\infty < x < \infty \\ \text{Interval Notation: } (-\infty, \infty) \end{array} \right]$$

Range:

$$\left[\begin{array}{l} \text{Solution: } f(x) \geq -45 \\ \text{Interval Notation: } [-45, \infty) \end{array} \right]$$