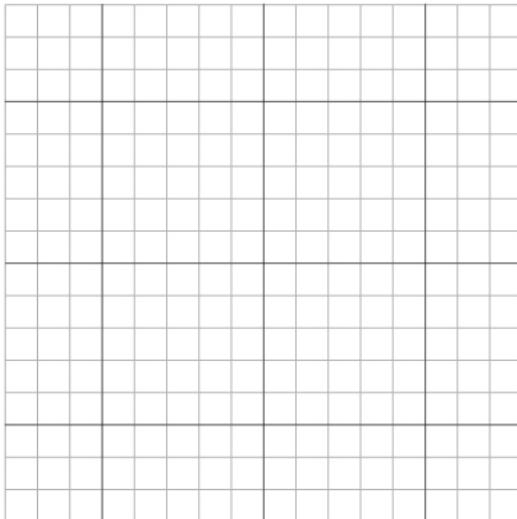


Analysis of Quadratic Functions

Find the vertex, x -and y -intercepts, domain and range of the given quadratic functions. Then, draw the graph.

① $f(x) = 2x^2 + 5x - 1$



Vertex:

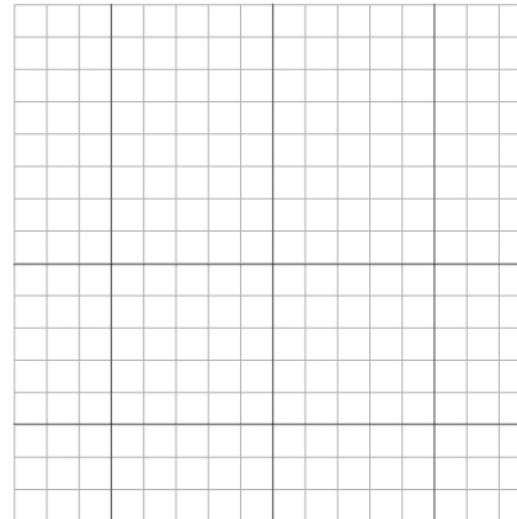
x -intercept:

y -intercept:

Domain:

Range:

② $f(x) = -x^2 + 3x - 6$



Vertex:

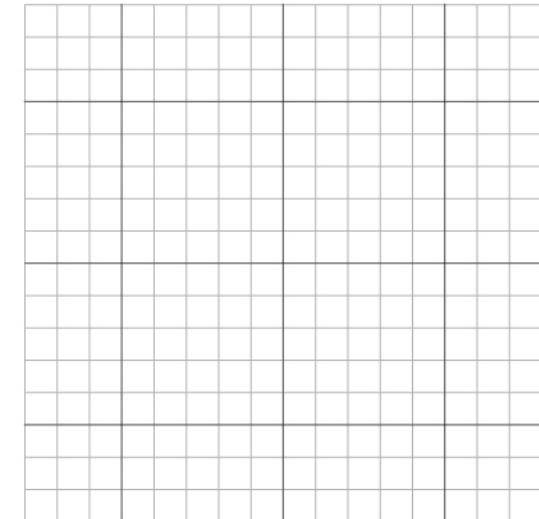
x -intercept:

y -intercept:

Domain:

Range:

③ $f(x) = x^2 + x - 12$



Vertex:

x -intercept:

y -intercept:

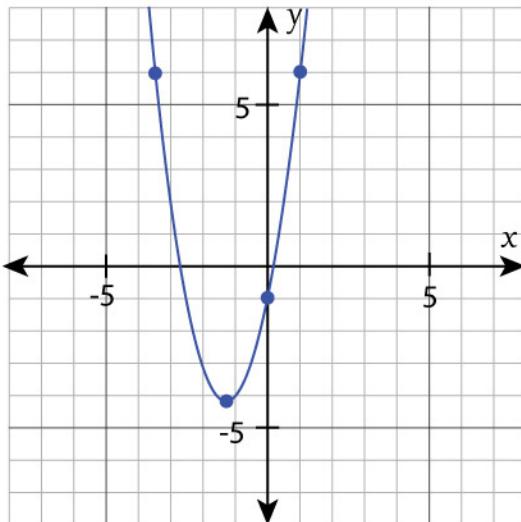
Domain:

Range:

Analysis of Quadratic Functions

Answers

① $f(x) = 2x^2 + 5x - 1$



Vertex: $\left(-\frac{5}{4}, -\frac{33}{8}\right)$

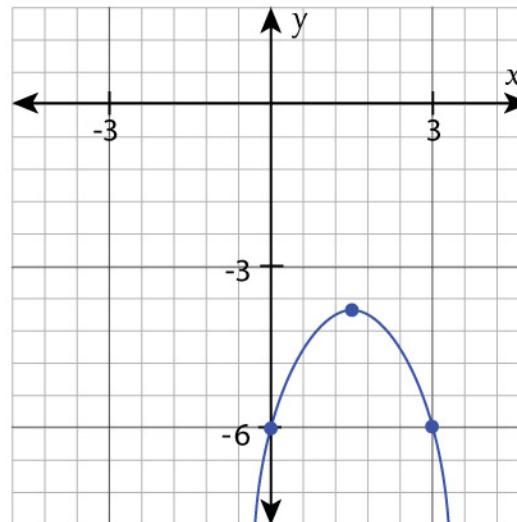
x -intercept: $\left(\frac{-5 + \sqrt{33}}{4}, 0\right), \left(\frac{-5 - \sqrt{33}}{4}, 0\right)$

y -intercept: $(0, -1)$

Domain: $\begin{bmatrix} \text{Solution: } -\infty < x < \infty \\ \text{Interval notation: } (-\infty, \infty) \end{bmatrix}$

Range: $\begin{bmatrix} \text{Solution: } f(x) \geq -\frac{33}{8} \\ \text{Interval notation: } \left[-\frac{33}{8}, \infty\right) \end{bmatrix}$

② $f(x) = -x^2 + 3x - 6$



Vertex: $\left(\frac{3}{2}, -\frac{15}{4}\right)$

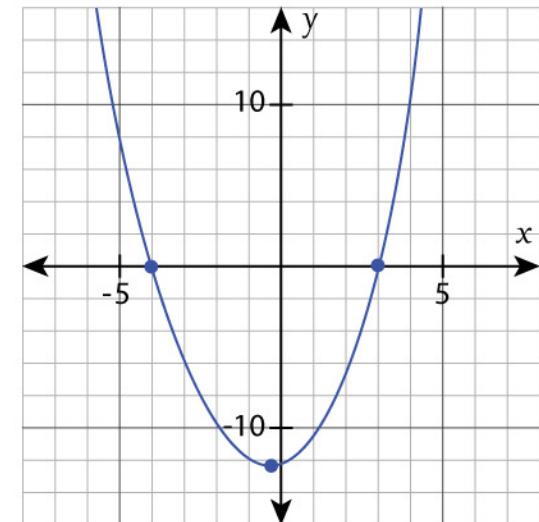
x -intercept: No x -intercept

y -intercept: $(0, -6)$

Domain: $\begin{bmatrix} \text{Solution: } -\infty < x < \infty \\ \text{Interval notation: } (-\infty, \infty) \end{bmatrix}$

Range: $\begin{bmatrix} \text{Solution: } f(x) \leq -\frac{15}{4} \\ \text{Interval notation: } \left(-\infty, -\frac{15}{4}\right] \end{bmatrix}$

③ $f(x) = x^2 + x - 12$



Vertex: $\left(-\frac{1}{2}, -\frac{49}{4}\right)$

x -intercept: $(3, 0), (-4, 0)$

y -intercept: $(0, -12)$

Domain: $\begin{bmatrix} \text{Solution: } -\infty < x < \infty \\ \text{Interval notation: } (-\infty, \infty) \end{bmatrix}$

Range: $\begin{bmatrix} \text{Solution: } f(x) \geq -\frac{49}{4} \\ \text{Interval notation: } \left[-\frac{49}{4}, \infty\right) \end{bmatrix}$